



Sparse 2D SAR apertures for 3D SAR

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Introduction

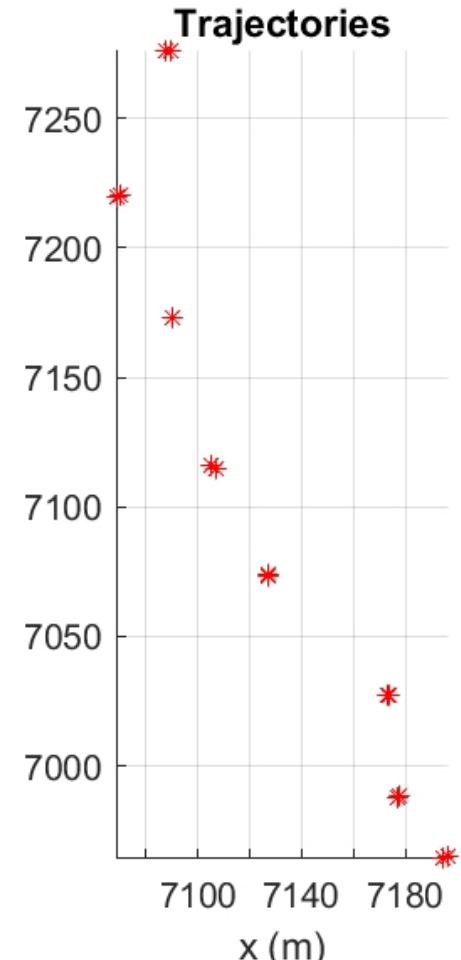
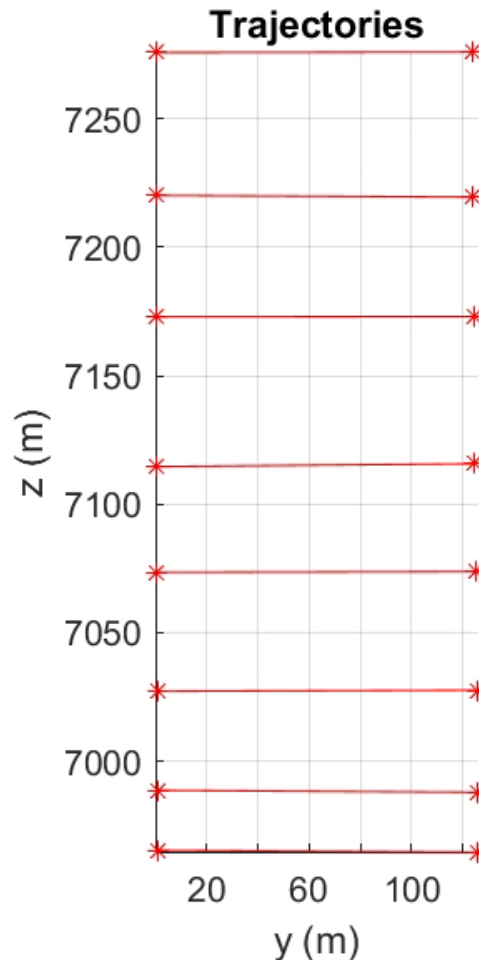
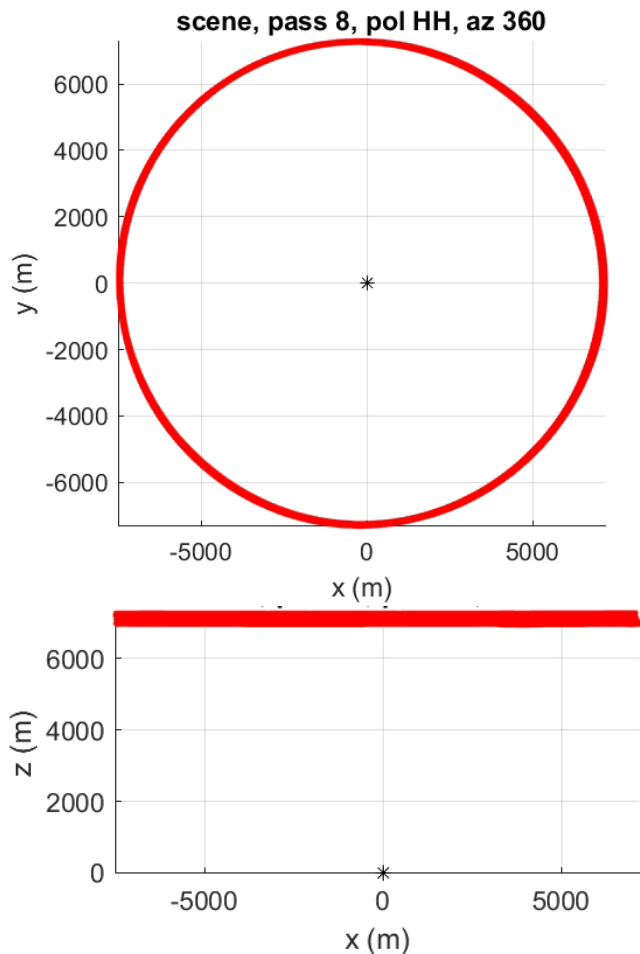
- There is a need to **remotely** determine internal structures of buildings, detecting presence of equipment & human activity
 - Current techniques involve close contact of radar against wall.
- 3D LF SAR would penetrate walls & separate clutter
- Supporting Dstl programme: **Remote Intelligence of Building Interiors**
- Several strands of work ongoing including processing of airborne volumetric LF CSAR: Airbus/Dstl dataset





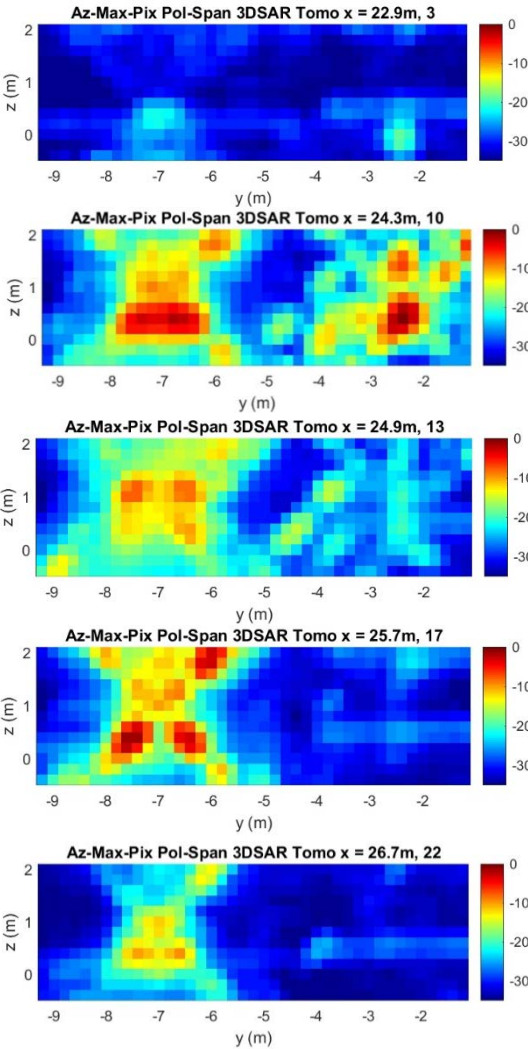
GOTCHA airborne 3D SAR

- We are working on MOCO for the Airbus CSAR dat
- In meantime we have been working on X-Band airborne 3DSAR image formation with the GOTCHA urban challenge dataset
 - Eight circular trajectories at different heights

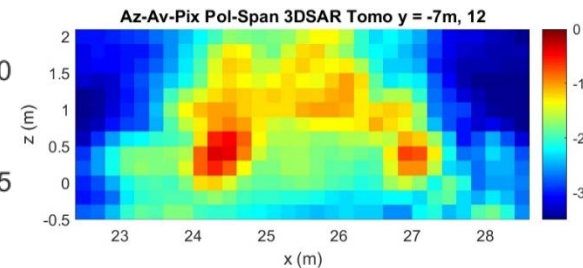
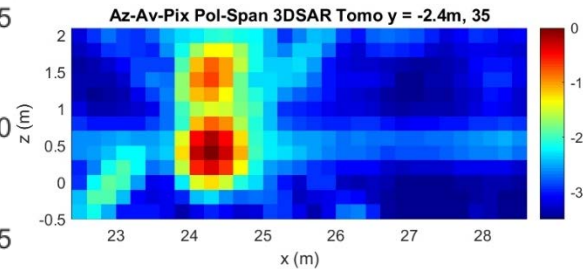
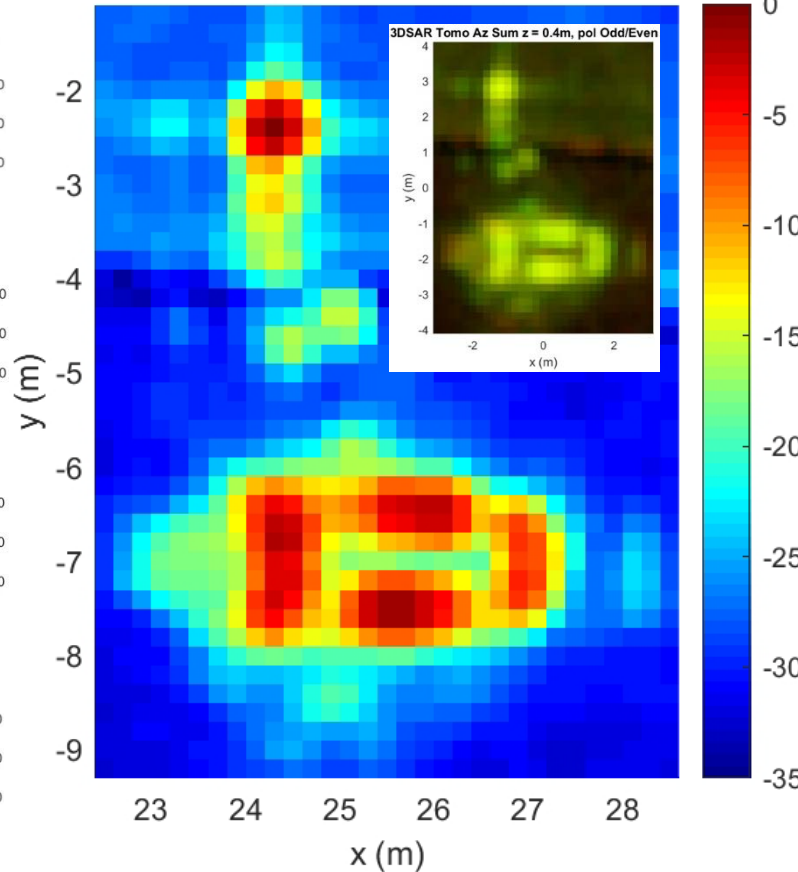




GOTCHA Airborne CSAR Fork lift truck tomograms



Az-Av-Pix Pol-Span 3DSAR Tomo z = 0.4m, 5

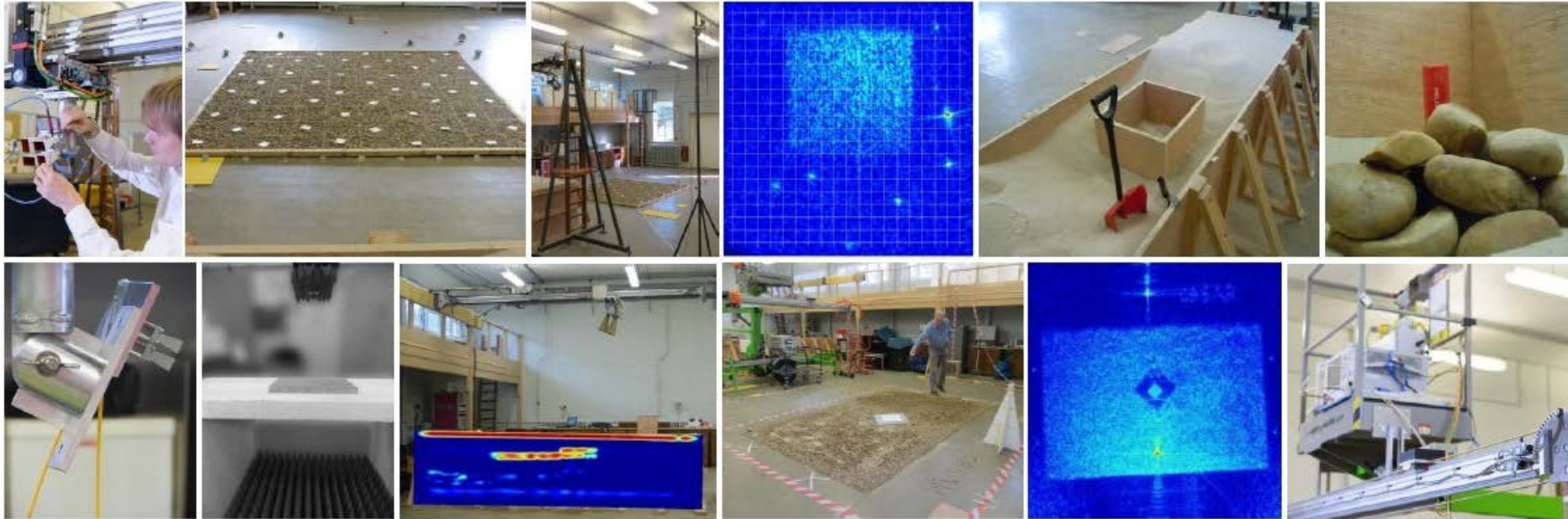




GBSAR System

The Indoor System

The indoor system is housed within a flexible 17m (l) x 9m (w) x 5m (h) laboratory workspace, which provides a highly controlled, precision, repeatable, 'radar-quiet' measurement environment. The system is currently figured to operate up to 26.5GHz, but can operate up to 50GHz for bespoke measurements. Radar imagery can be collected in both SAR and Tomographic Profiling modes, as well as reflectivity measurements for the determination of material properties. Numerous bi-static and multi-static configurations are available. Automation allows the system to collect large, continuous image sets for the study of slowly evolving scattering processes without the need for operator presence. The 4m x 1m x 1m sand trough is used in the study of sub-surface imaging phenomena.



SAR, bistatic SAR
500MHz – 40GHz

Polarisation: Full quad

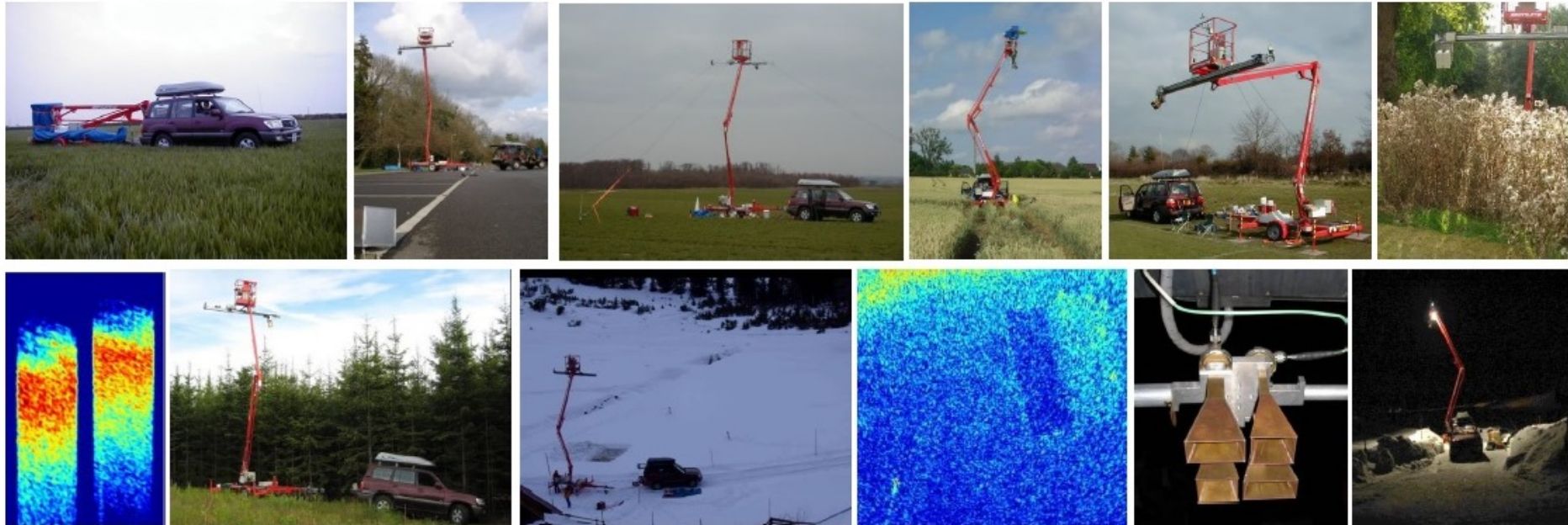
Nominal Accuracies: 1dB, 5°



GBSAR System

The Outdoor System

The outdoor system is a bespoke, portable outdoor radar imaging system. It consists of a trailer-mounted hoist, which is transported to site by a Land Cruiser 4x4 vehicle. For deployment, the horizontal scanning boom is attached to the basket and lifted to the chosen height. Imagery is collected by scanning the antenna sledge along the boom. The standard imaging modes are SAR and Tomographic Profiling (TP). The radar unit sits in the basket, and the whole system is controlled from a laptop at ground level. The antenna sledge can be offset front-back to provide an interferometric baseline. In addition, bespoke set-ups can collect bi-static imagery.



SAR, bistatic SAR 500MHz – 40GHz

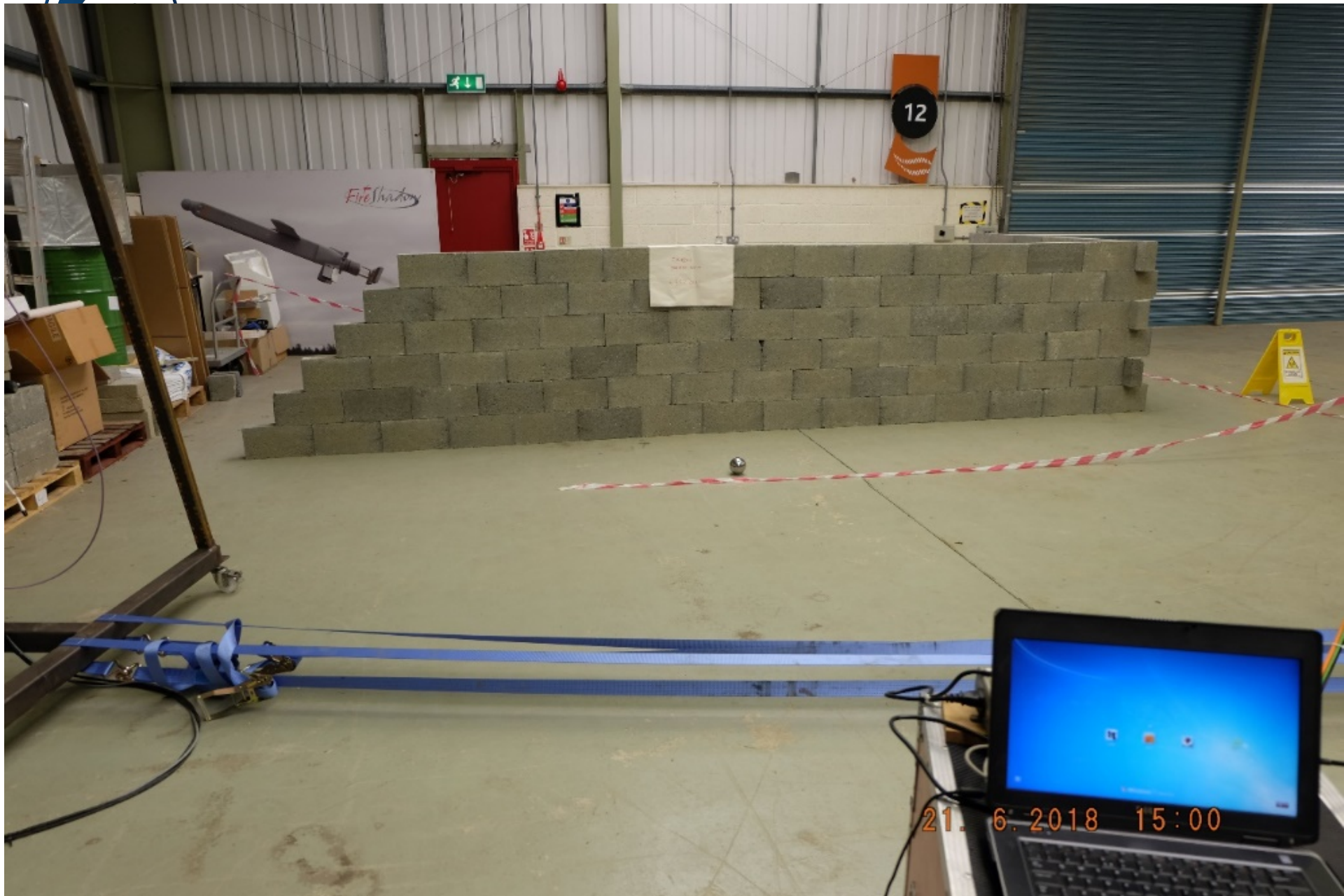
Polarisation: Full quad

Height: 0-10m

Nominal Accuracies: 1dB, 5°



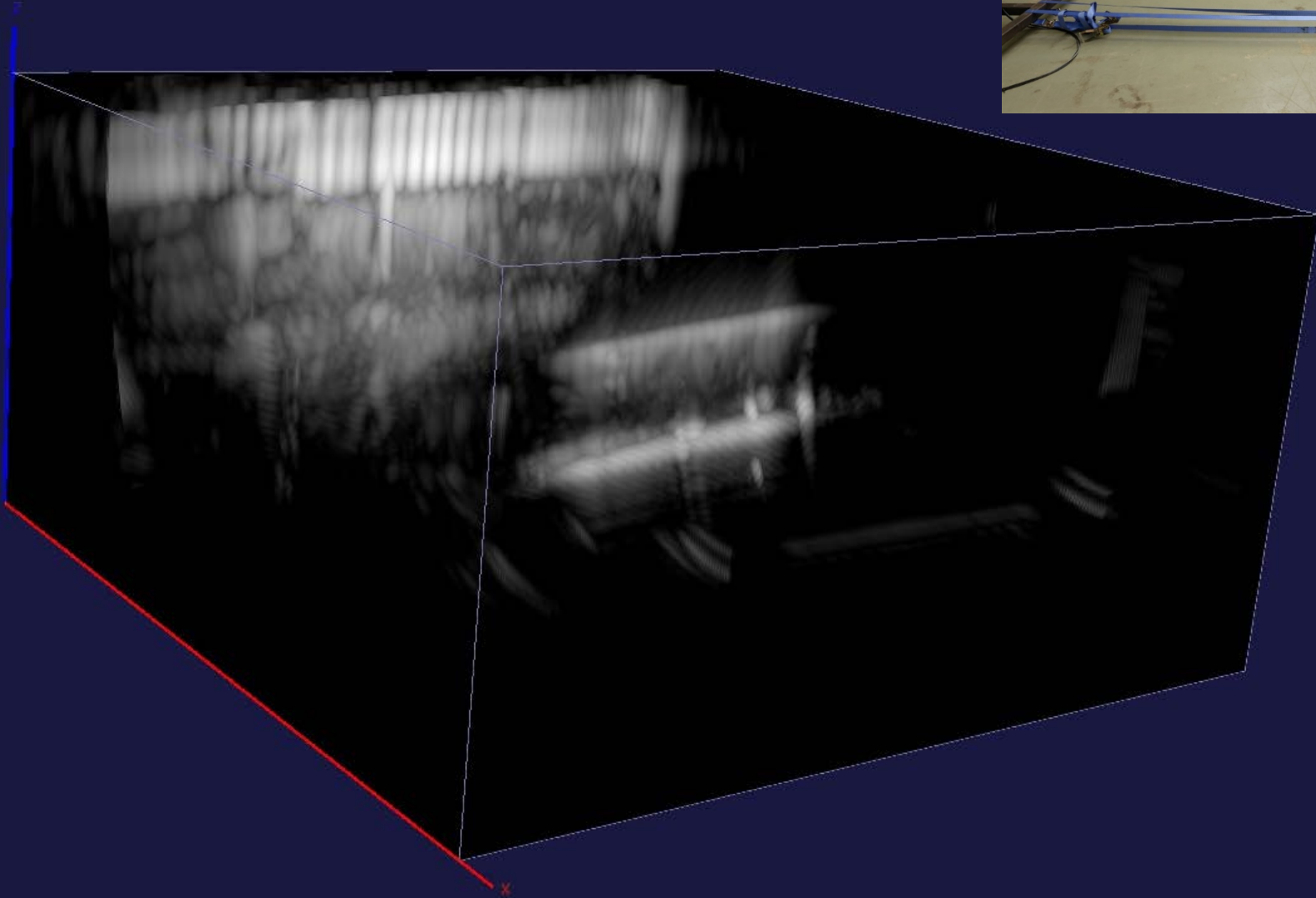
3D SAR of GBSAR Lab





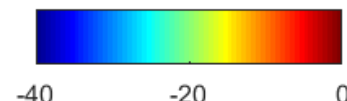
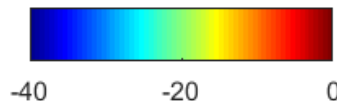
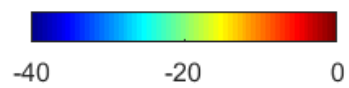
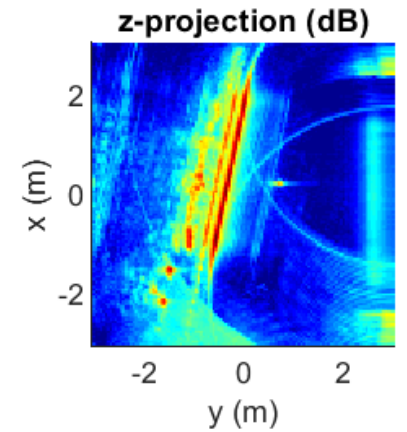
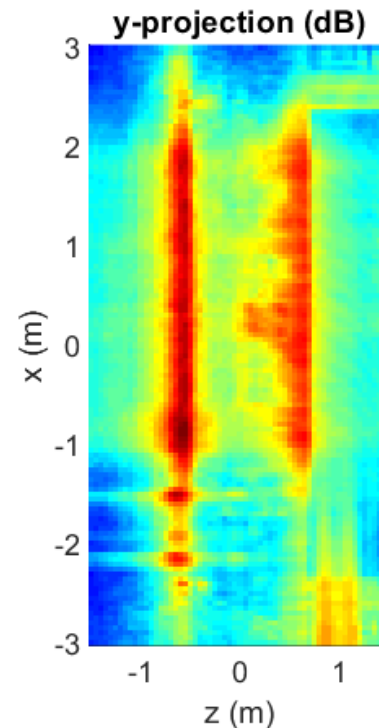
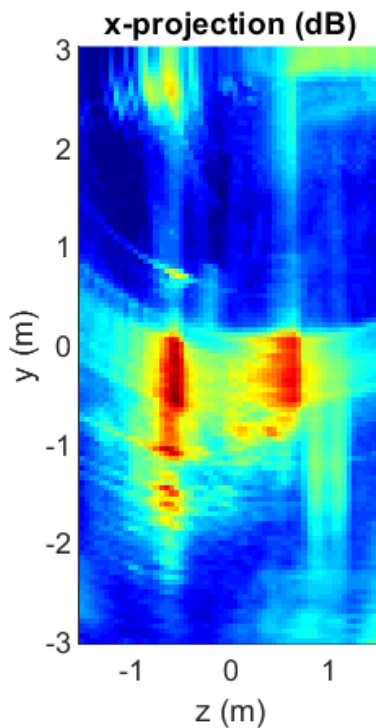
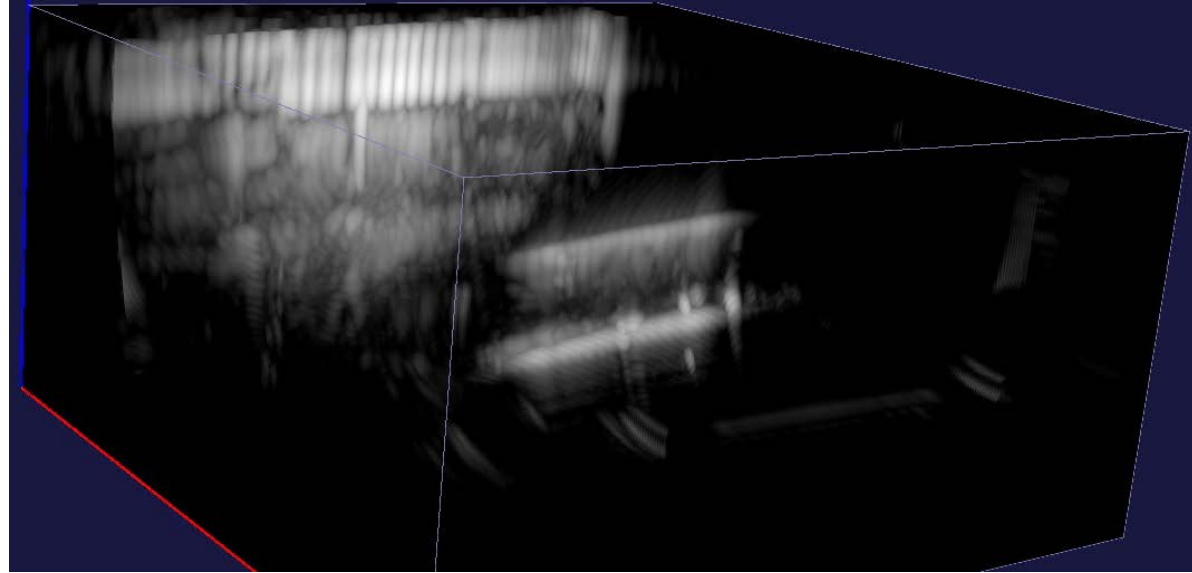
3D SAR of GBSAR Lab





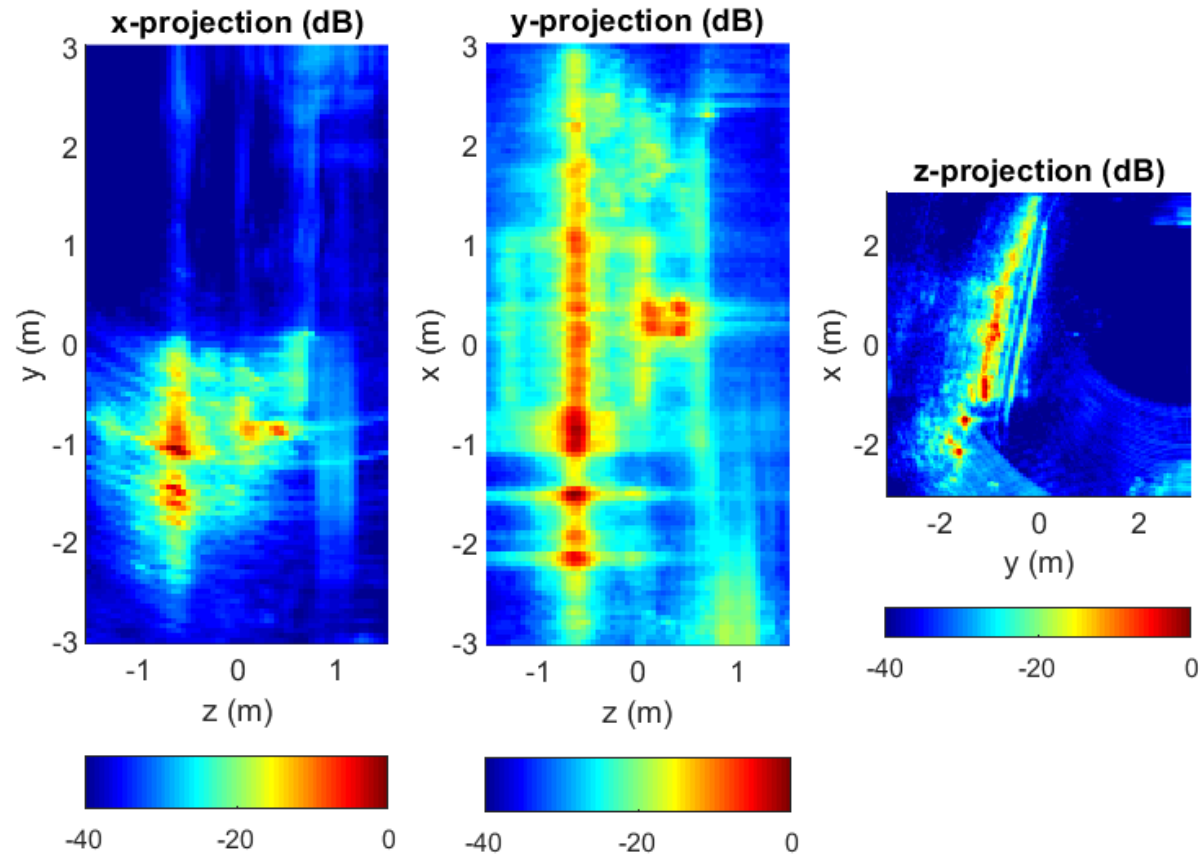
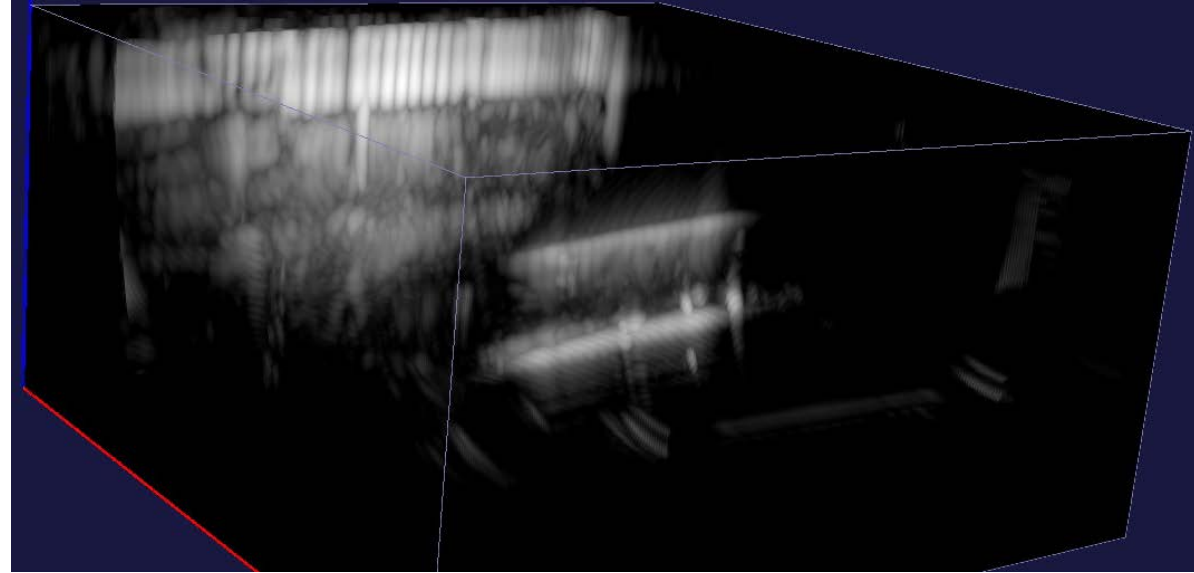
- Projections

- Barrels, multipath
- Briefcase
- Monitor
- Desk





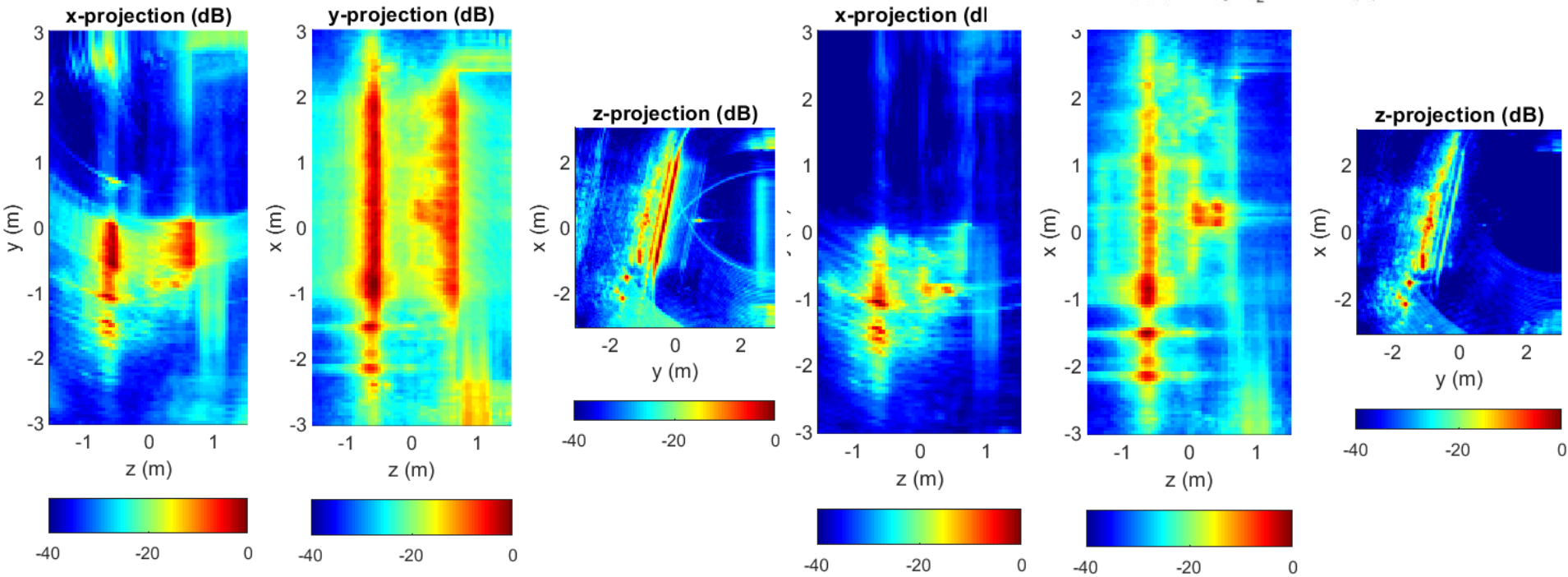
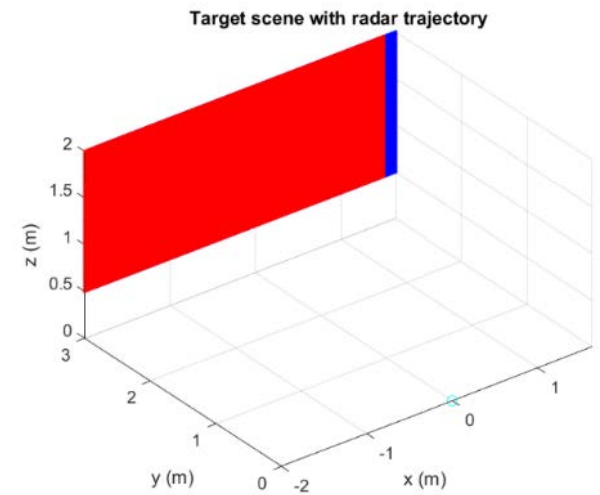
- Projections
- **Background subtracted**
 - Barrels, multipath
 - Briefcase
 - Monitor
 - Desk





Fully sampled 2D aperture

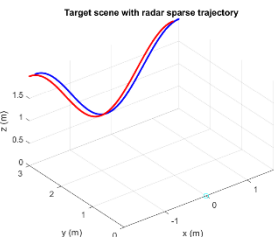
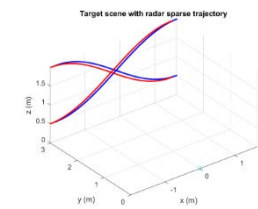
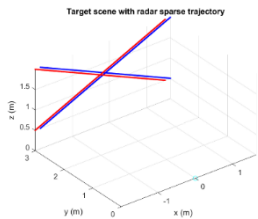
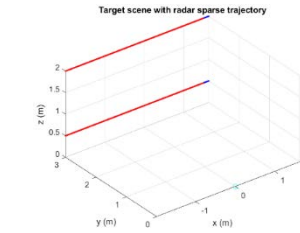
- 3D LF SAR of GBSAR Lab



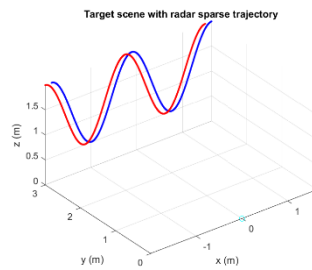
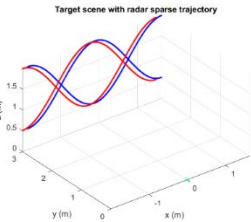
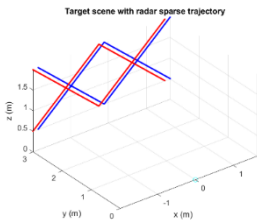
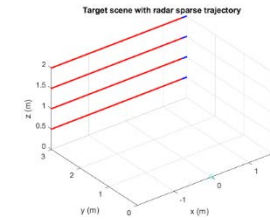
Background subtracted

Classes of sparse sampled trajectories

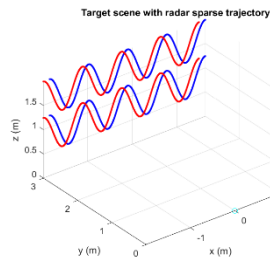
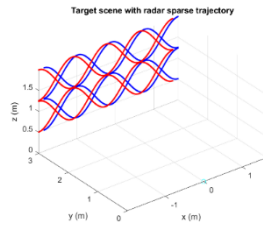
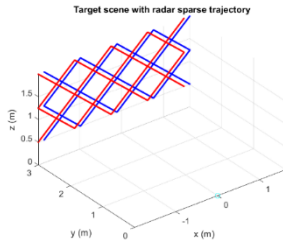
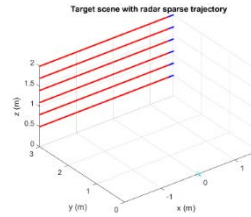
$N_y=0$



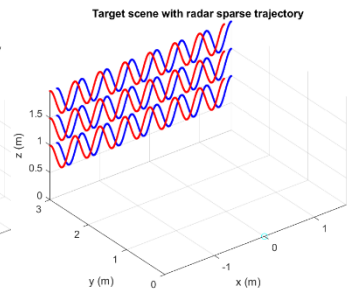
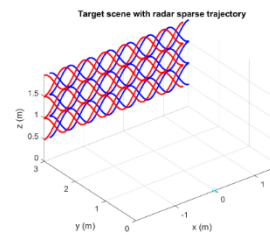
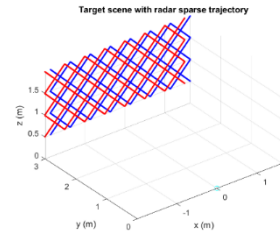
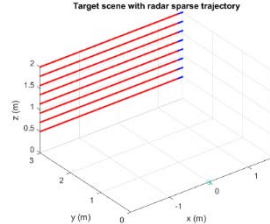
$N_y=1$



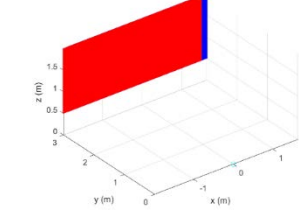
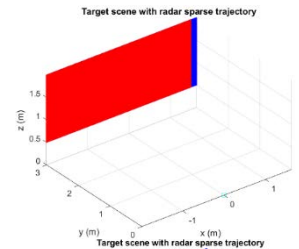
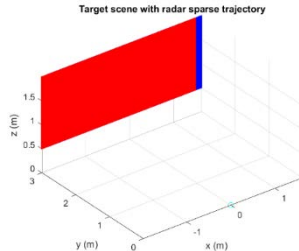
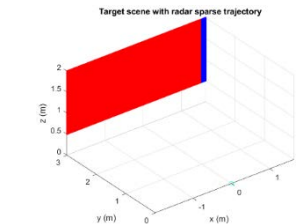
$N_y=2$



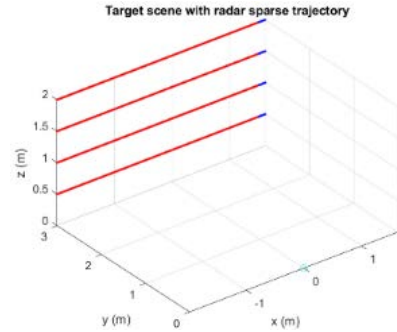
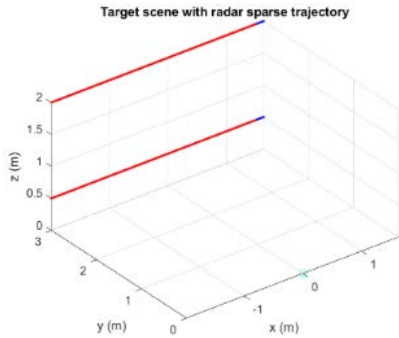
$N_y=3$



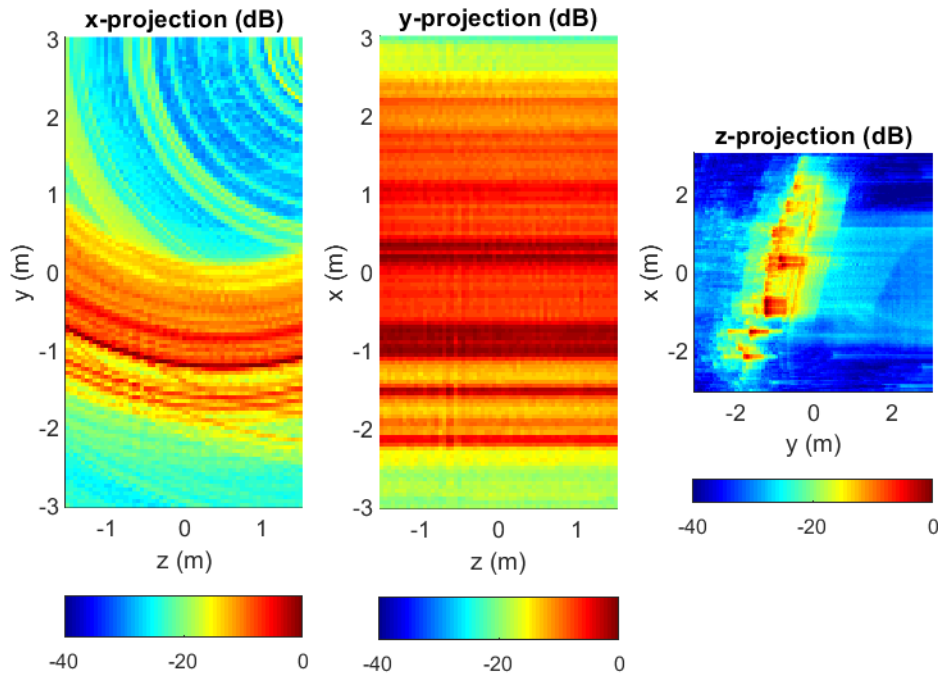
$N_y=38$



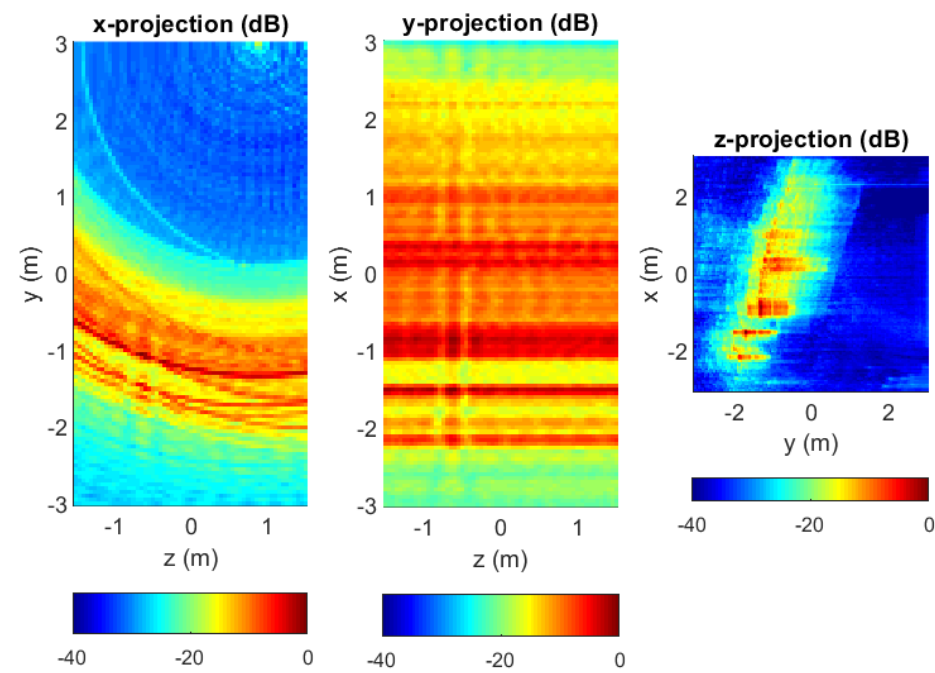
Repeat Linear pass



Sparse RL
2 passes, bg-s

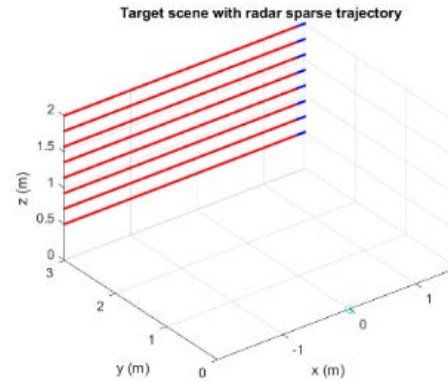
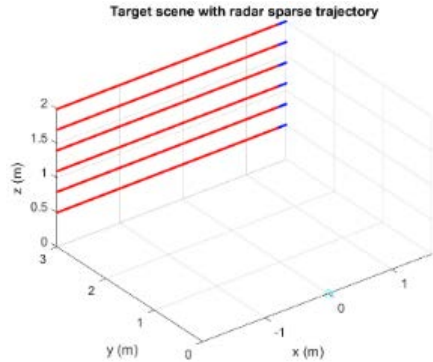


Sparse RL
4 passes, bg-s



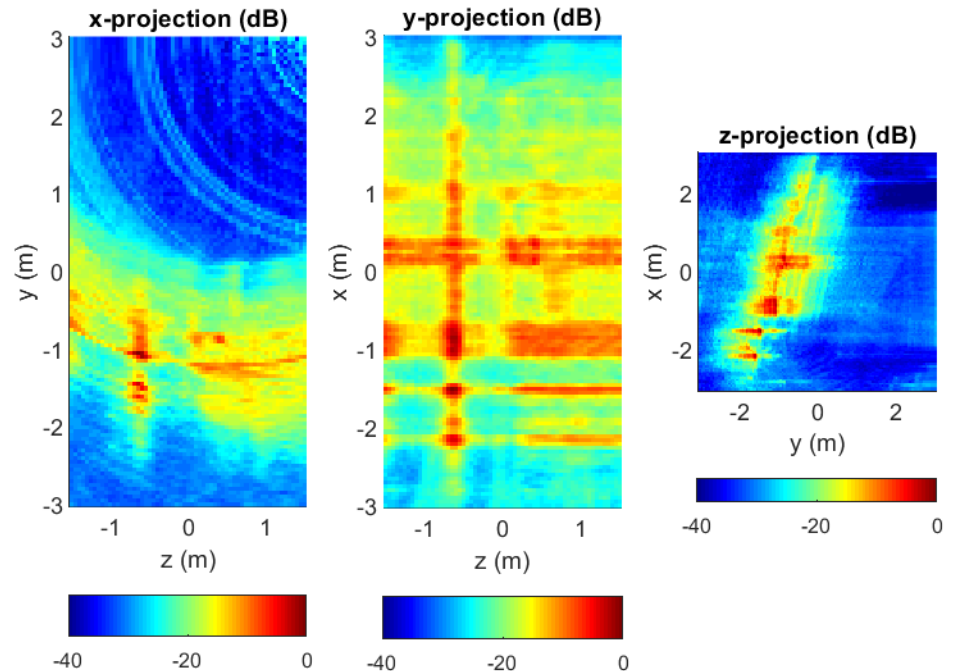
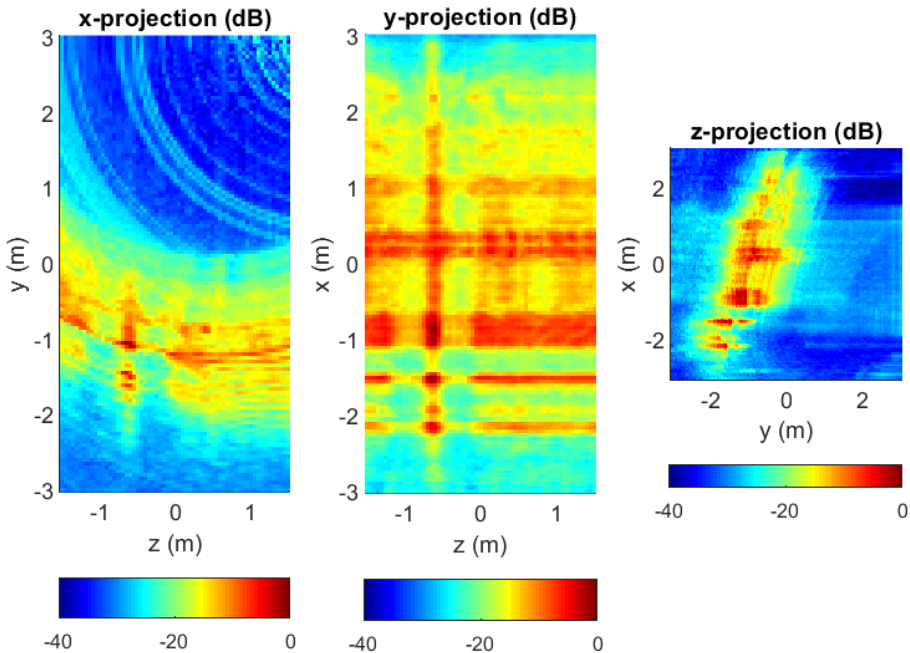


Repeat Linear pass



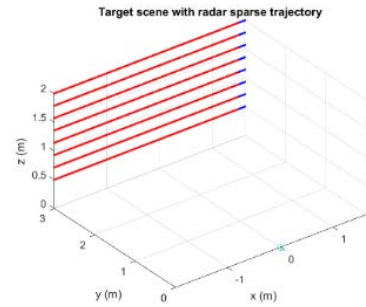
Sparse RL
6 passes, bg-s

Sparse RL
8 passes, bg-s

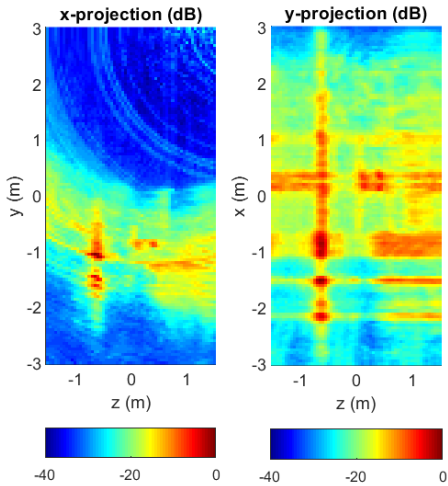




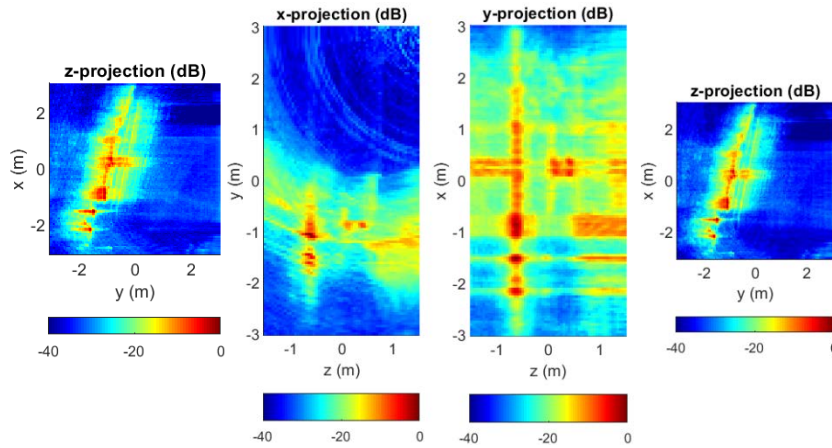
Repeat Linear pass



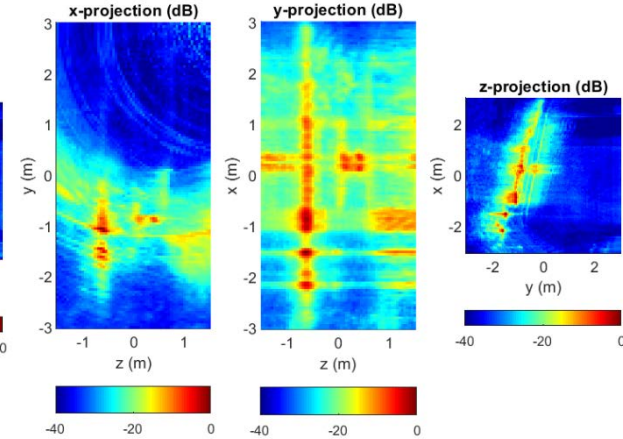
Sparse RL 10 passes bg-s



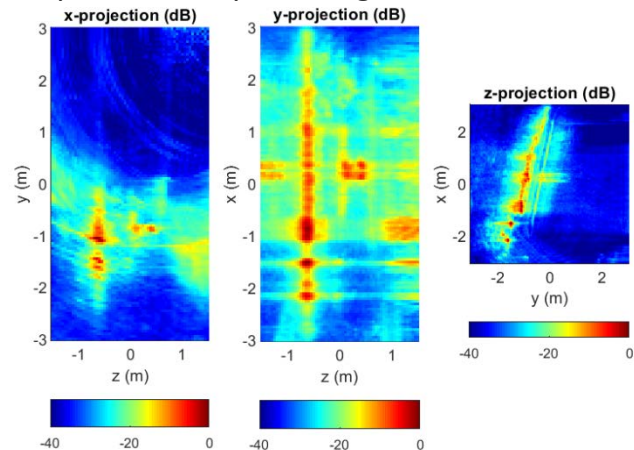
Sparse RL 12 passes bg-s



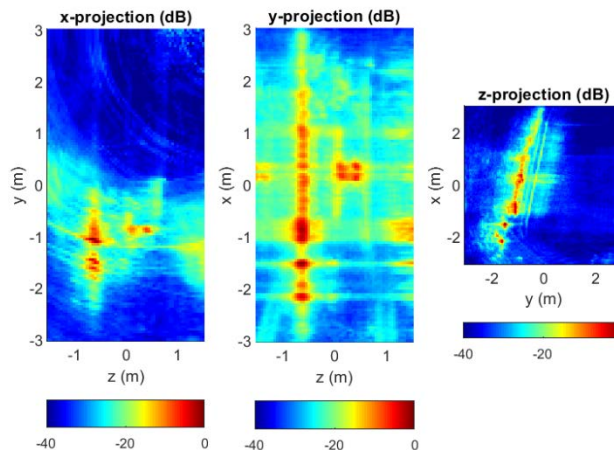
Sparse RL 14 passes bg-s



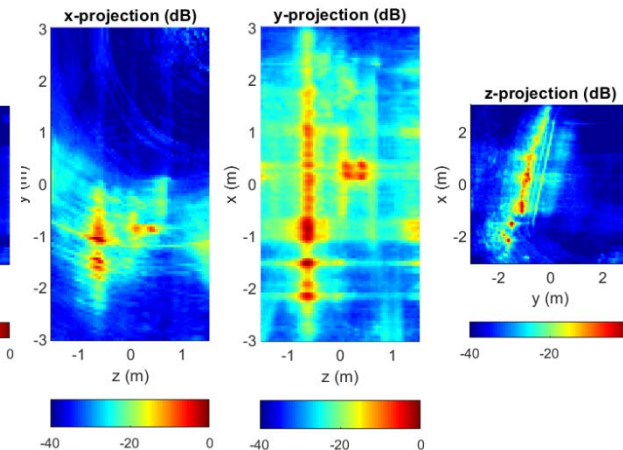
Sparse RL 16 passes bg-s



Sparse RL 18 passes bg-s



Sparse RL 20 passes bg-s



Nyquist Sampling

(1) Vertical Nyquist sampling:

$$\theta_s f_c = c / (2 L_z)$$

(2) Range-angle:

$$z_d = R \theta_s$$

(3) Vertical Aperture division:

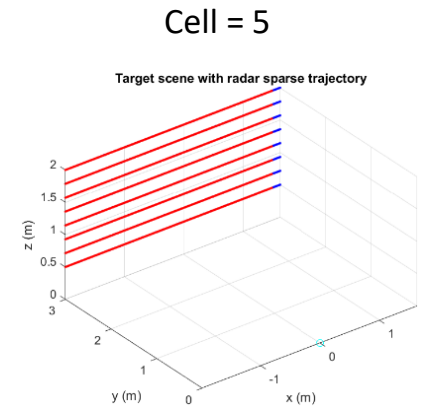
$$z_d = A_z / (N_z - 1)$$

Combining: $A_z / (N_z - 1) = R \theta_s = R c / (2 L_z f_c)$
 $N_z = 2 A_z f_c / (R c) L_z + 1$
 $N_z = B L_z + 1$

Setting: $A_z = 1.5\text{m}$, $f_c = 3.5\text{GHz}$, $R = 4\text{m}$, $c = 0.3\text{Gm/s}$

$$B = 2 * 1.5 * 3.5 / 4 / 0.3 = 8.75$$

$$\underline{N_z = 8.75 L_z + 1}$$

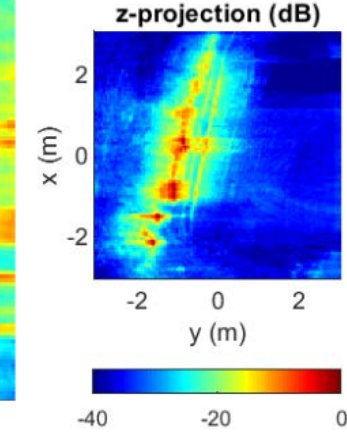
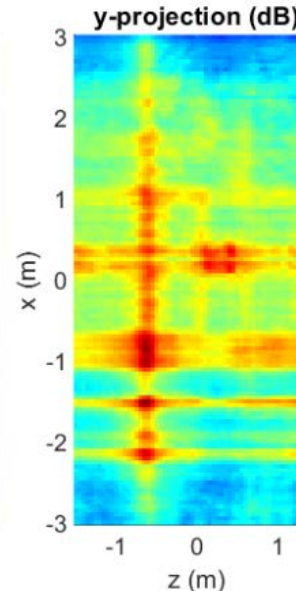
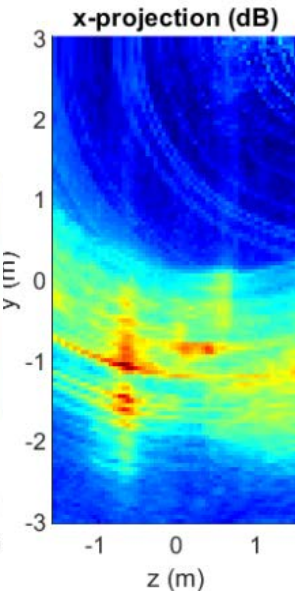
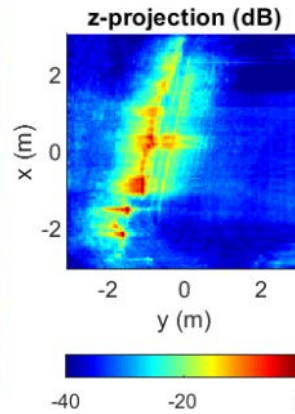
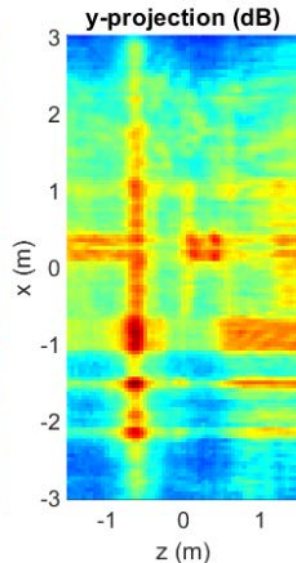
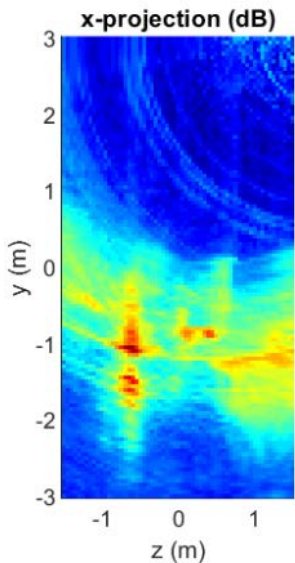
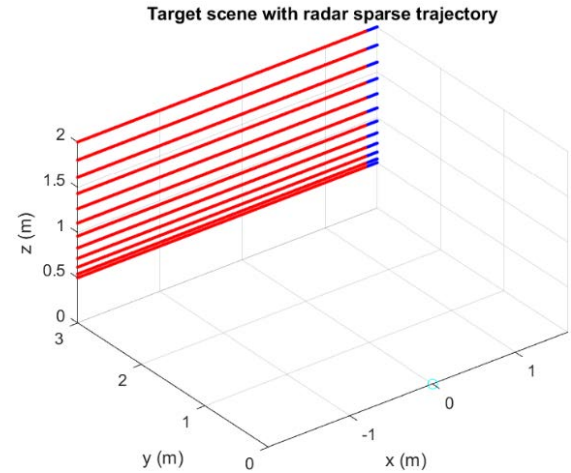
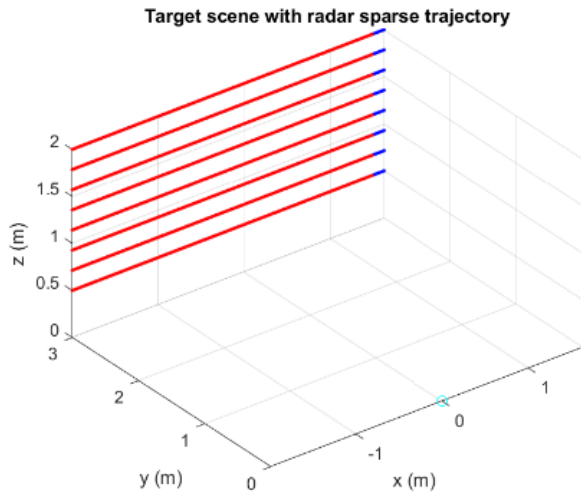


Lz (m)	Nz (frac)	Nz
0.5	5.4	6
1	9.8	10
1.5	14.1	15
2	18.5	19
2.5	22.9	23

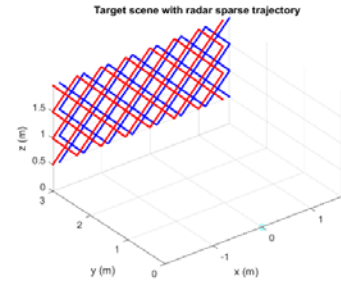


Repeat linear pass, nonlinear in height

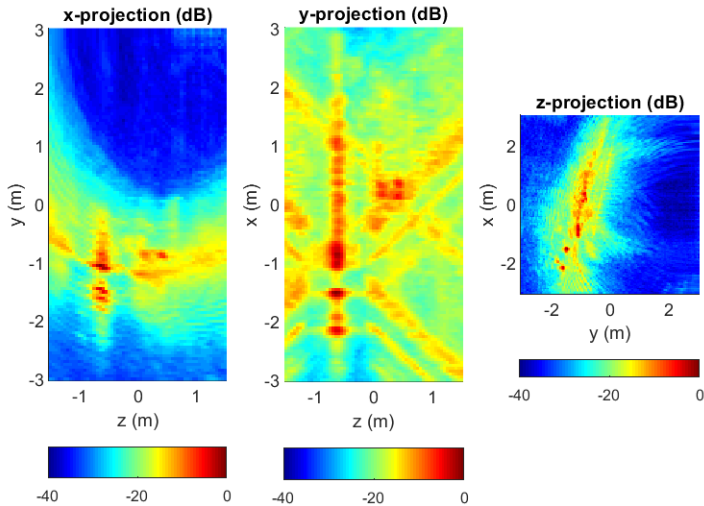
To attempt to spread aliased energy, try nonlinear spacing in height



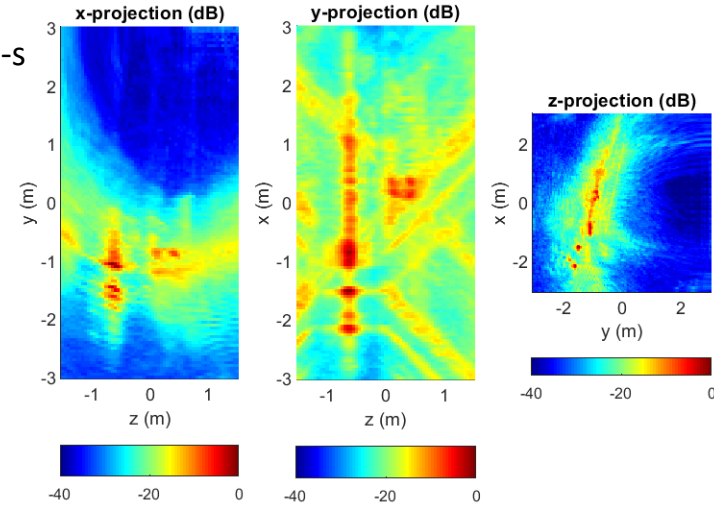
Crossed Linear pass



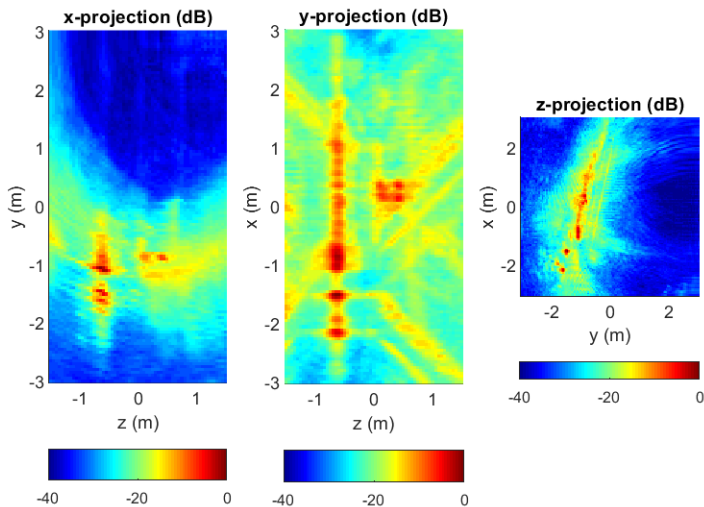
C=1 NY=5 bg-s



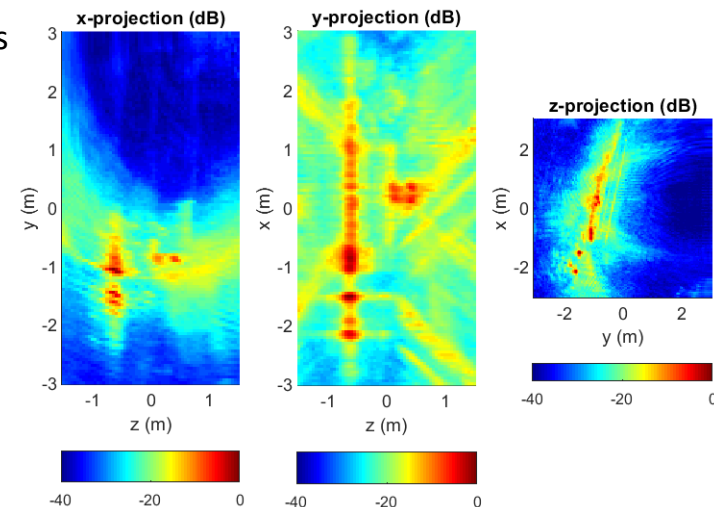
C=1 NY=6 bg-s



C=1 NY=7 bg-s



C=1 NY=8 bg-s



Nyquist Sampling

(1) diagonal Nyquist sampling: $\theta_s f_c = c / (2 L_d)$

(2) Range-angle: $l_d = R \theta_s$

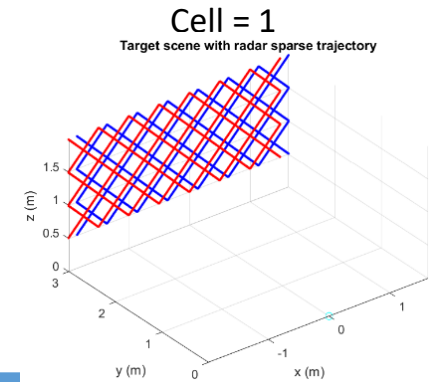
(3) Vertical Aperture division: $l_d = A_d / (N_d - 1)$

Combining: $A_d / (N_d - 1) = R \theta_s = R c / (2 L_d f_c)$
 $N_d = 2 A_d f_c / (R c) L_d$
 $N_d = B L_z$

Setting: $A_d = 1.5/\sqrt{2}=1.1\text{m}$, $f_c = 3.5\text{GHz}$, $R = 4\text{m}$, $c = 0.3\text{Gm/s}$

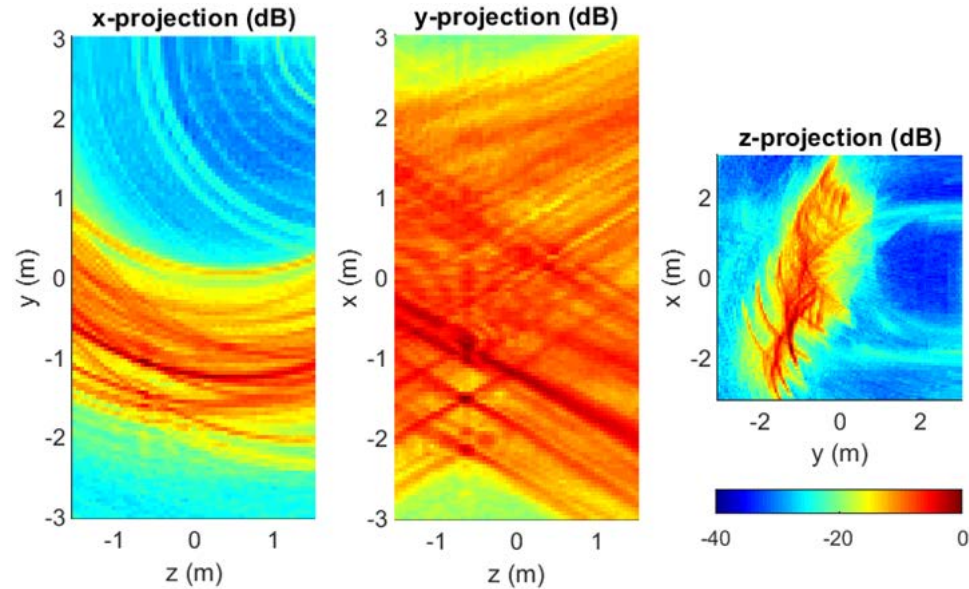
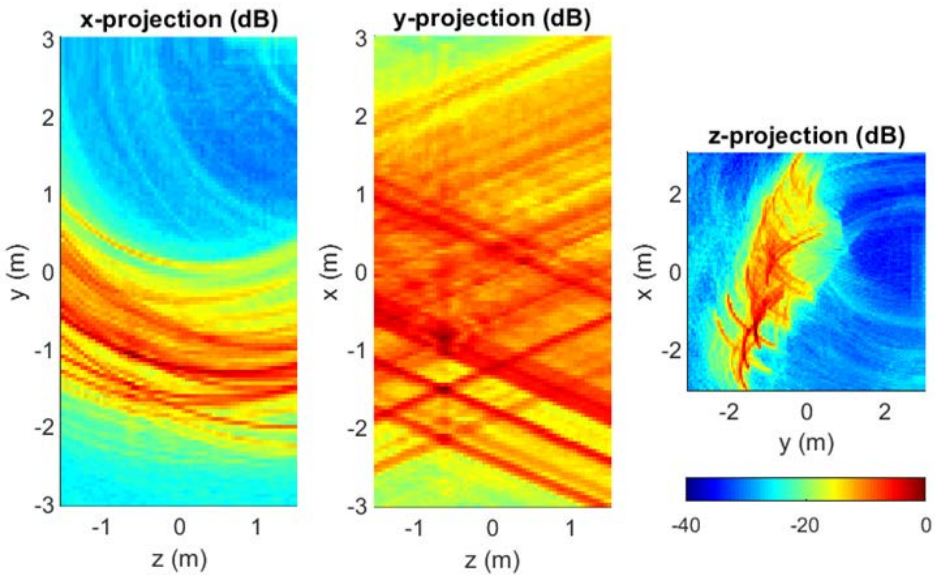
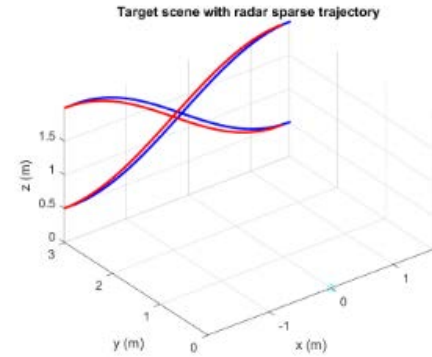
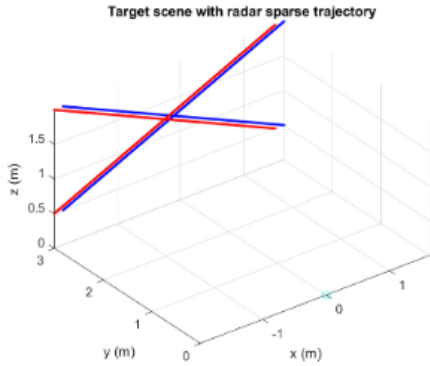
$$B = 2 * 1.5 * 3.5 / 4 / 0.3 = 6.19$$

$$\underline{N_z = 6.19 L_z}$$

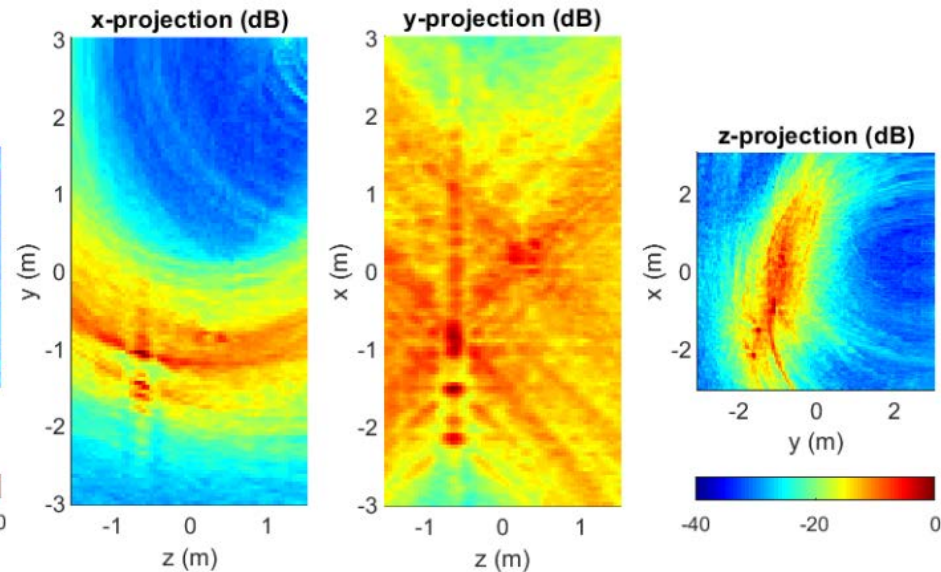
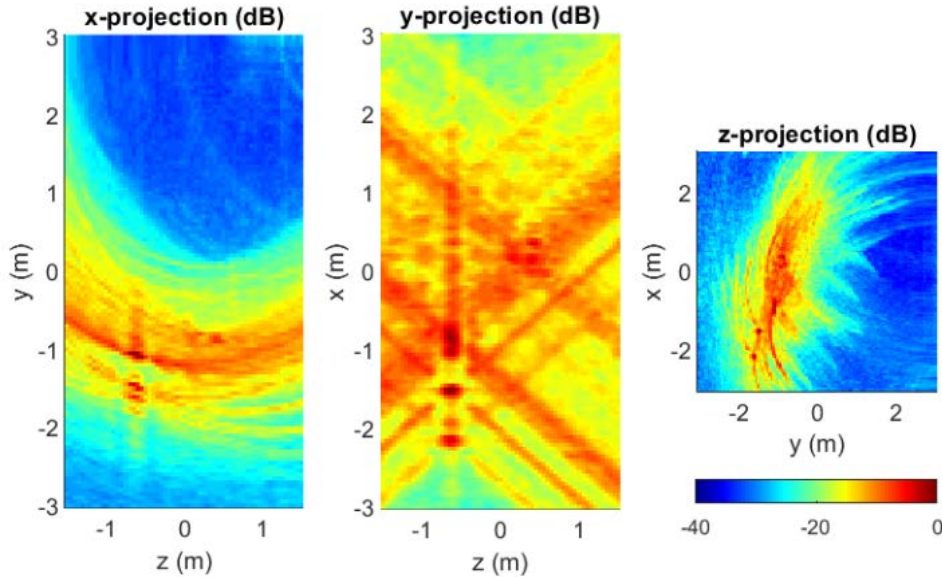
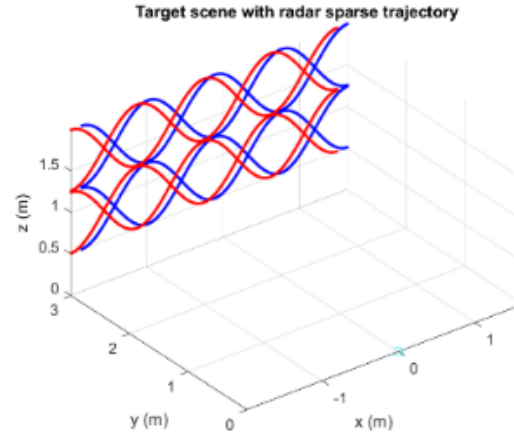
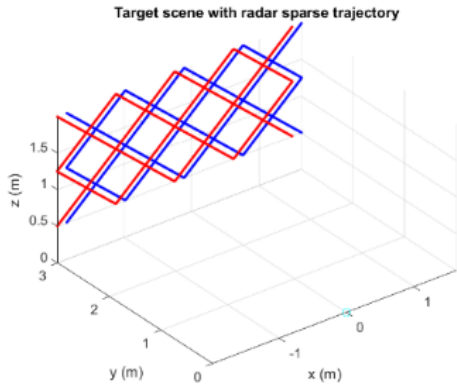


Ld (m)	Nd (frac)	Nd
0.5	3.1	4
1	6.2	7
1.5	9.3	10
2	12.4	13
2.5	15.5	16
3	18.6	19
3.5	21.7	22

Crossed Linear and Sinusoid pass



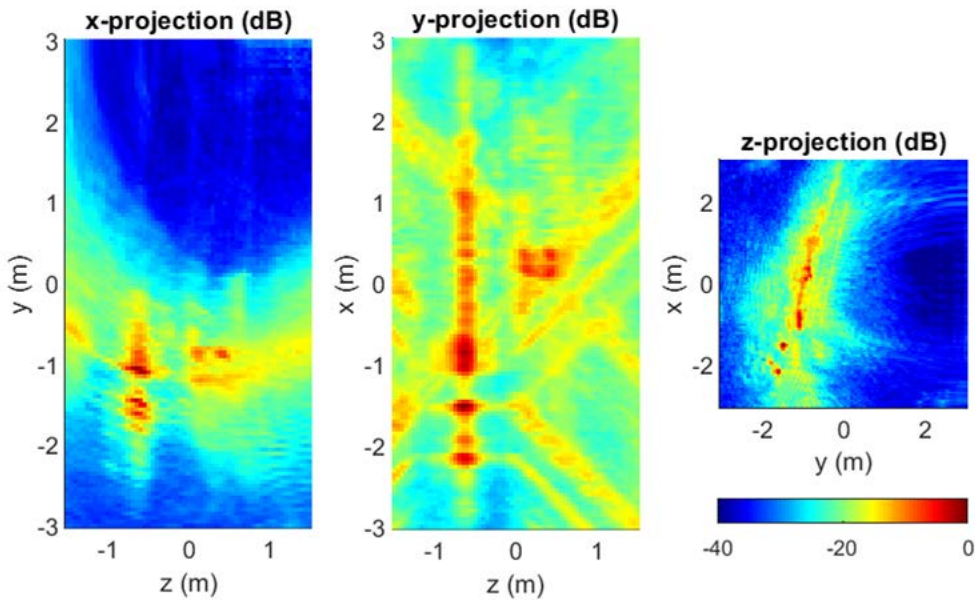
Crossed Linear and Sinusoid pass



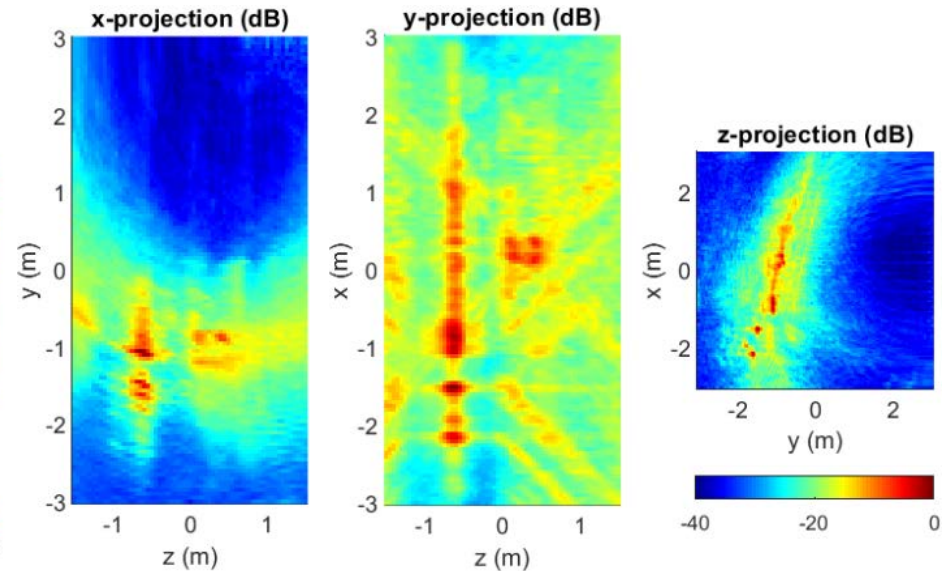
Sparse CL 4 passes 2*4 crosses

Sparse CS 4 passes 2*4 crosses

Crossed Linear and Sinusoid pass

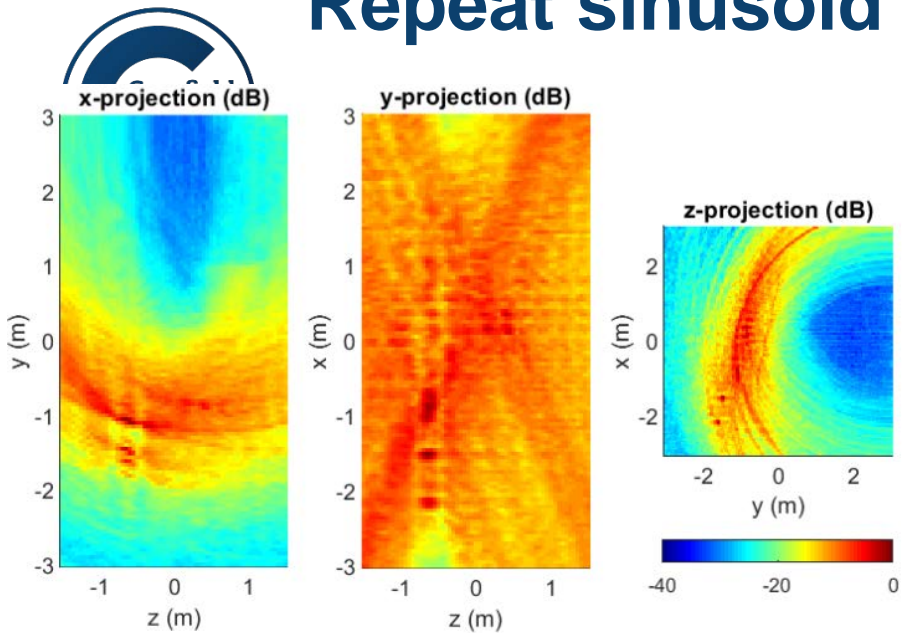


Sparse CL 12 passes 6*14 crosses

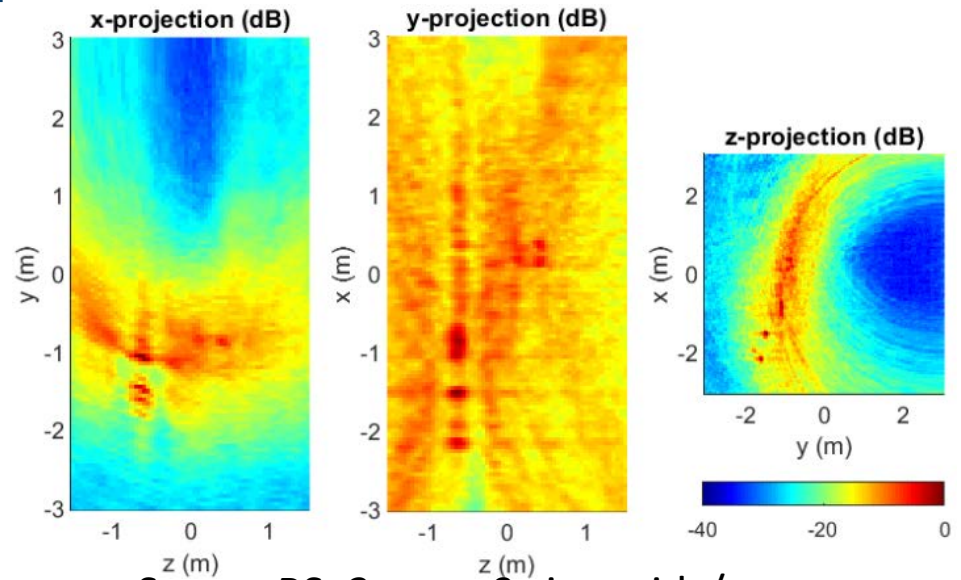


Sparse CS 12 passes 6*14 crosses

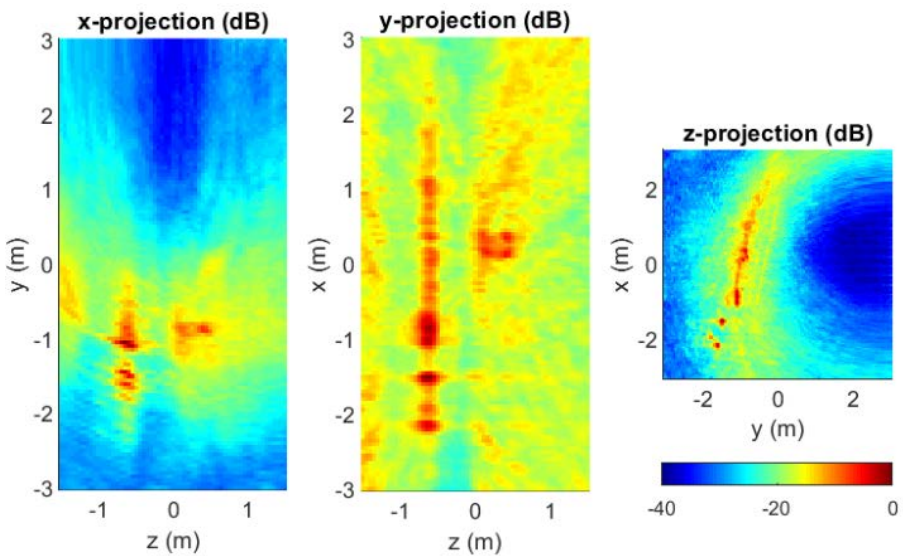
Repeat sinusoid pass



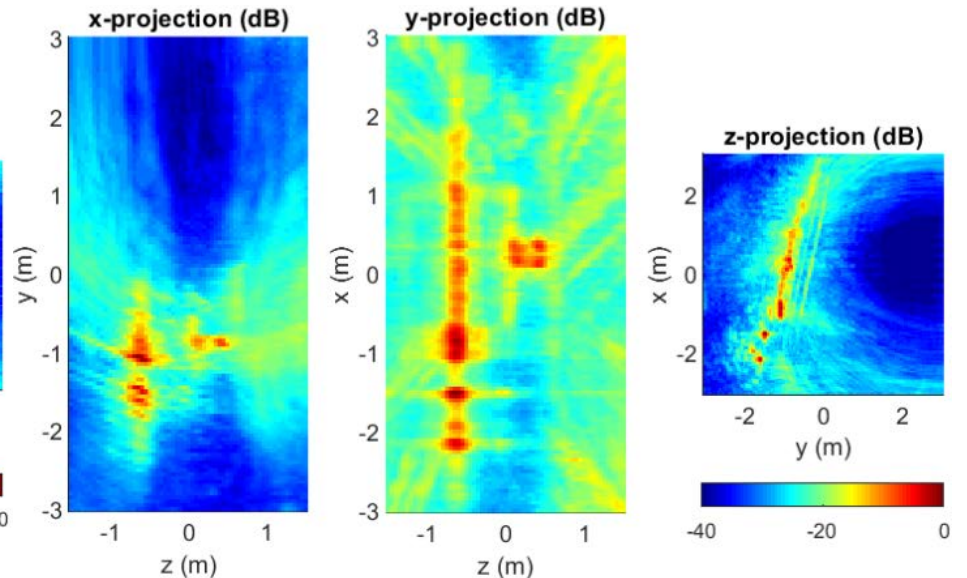
Sparse RS, 2 pass, 4 sinusoids/pass



Sparse RS, 3 pass, 9 sinusoids/pass

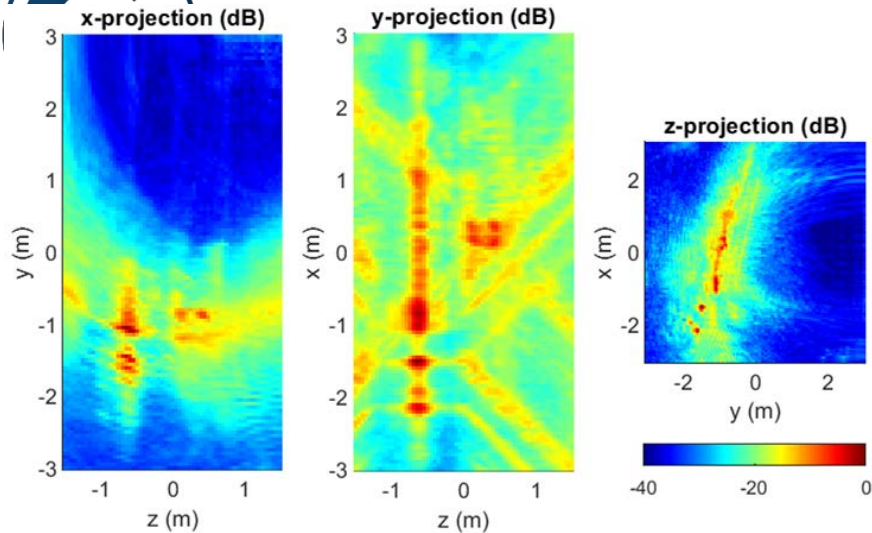
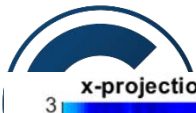


29 Sparse RS, 6 pass, 14 sinusoids/pass

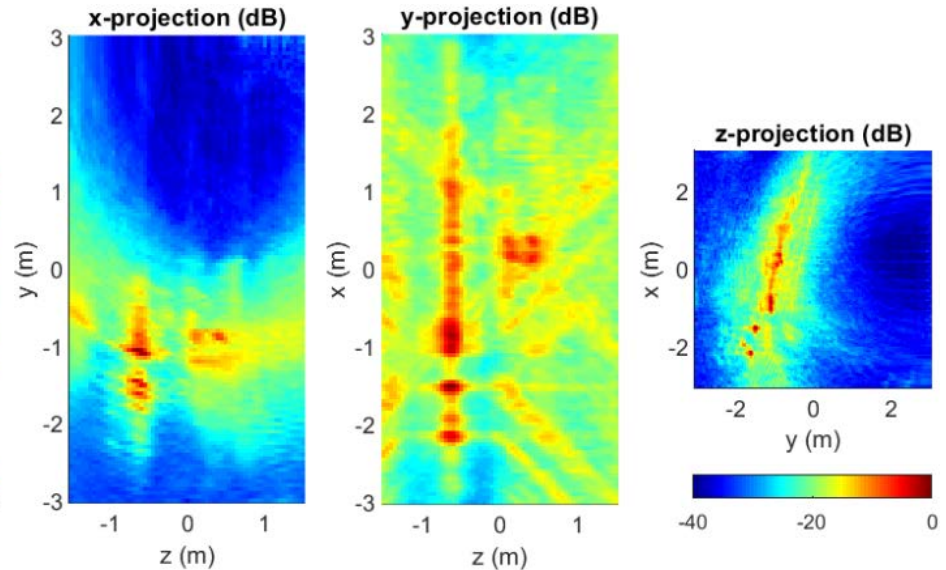


Sparse RS, 12 pass, 28 sinusoids/pass

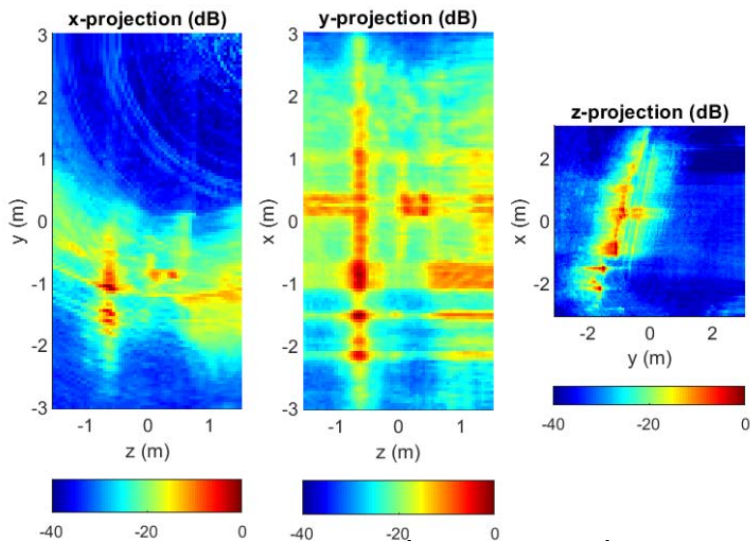
Comparison of 12 pass casses



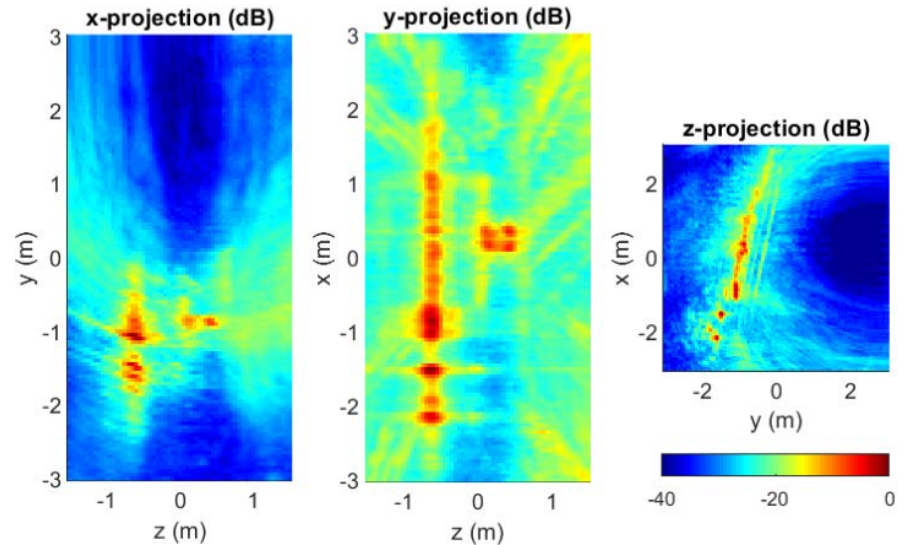
Sparse CL 12 passes 6*14 crosses



Sparse CS 12 passes 6*14 crosses



30 Sparse RL NY=6 (12 passes)

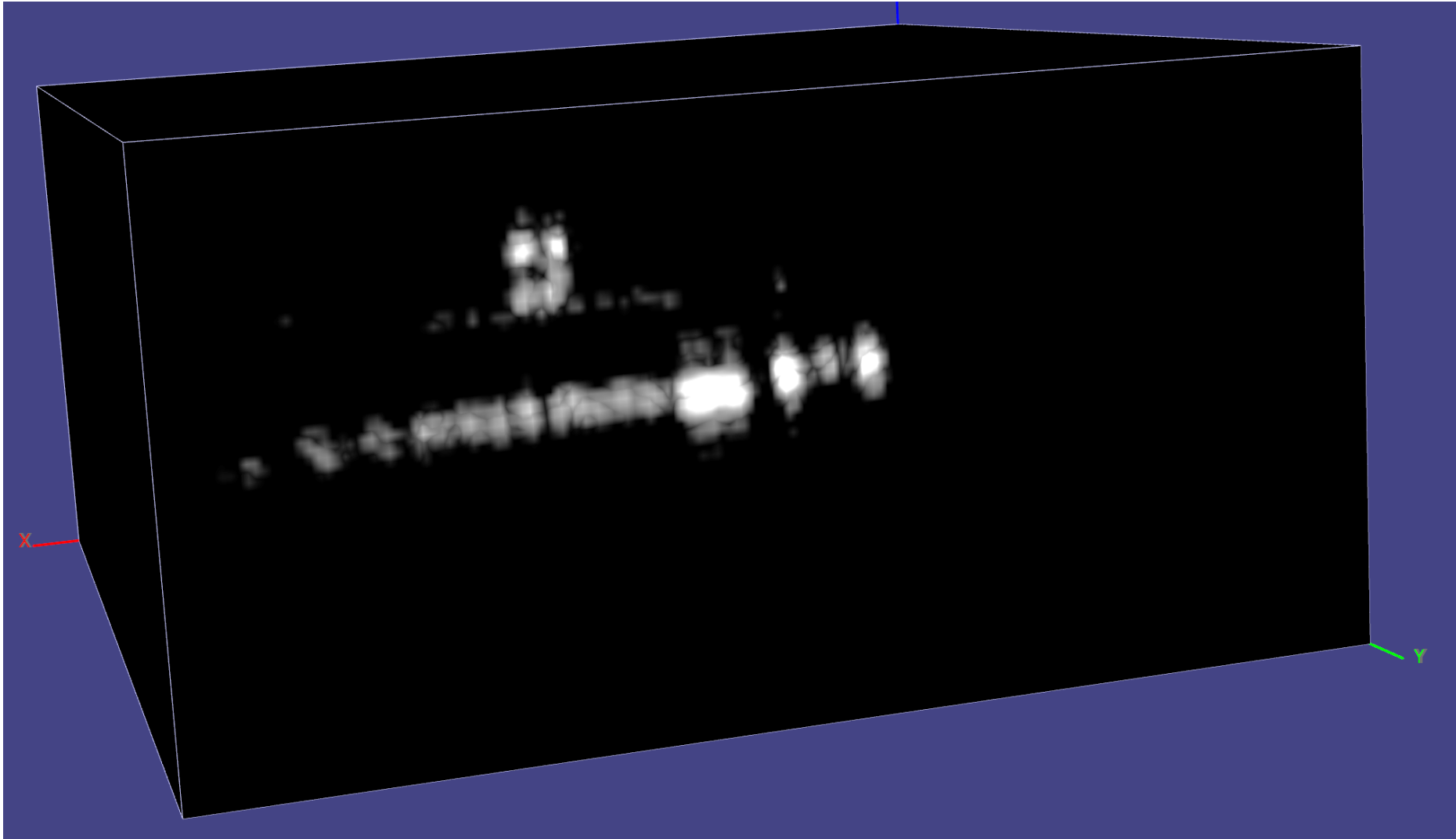


Sparse RS, 12 pass, 28 sinusoids/pass



12 repeat sinusoid pass

12 repeat sinusoids, giving at least 15dB artefact free dynamic range





Conclusion

- The resolution is mostly set by the overall aperture sizes;
- However aliased energy is dependent on the density of trajectories.
- If the aliased energy is spread out, then the max intensity of the aliased energy is reduced, giving an artefact free dynamic range.
- Crossed linear trajectories lead to spreading out of energy.
 - Curved crosses lead to further spreading out.
- The repeat pass sinusoid path seems to spread aliased energy the most, such that the higher the density of trajectory, the larger the artefact free dynamic range.
- No doubt many other useful sparse trajectories exist, and the key seems to be to spread out aliased energy.

A photograph of a field at sunset. In the foreground on the left, a large crane is silhouetted against the sky. The sun is low on the horizon, creating a bright orange and yellow glow. In the distance, three wind turbines are visible against the horizon. The sky is filled with scattered clouds, some of which are illuminated by the setting sun.

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